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Does Seasonality Change over the Business Cycle? An Investigation using Monthly Industrial Production Series

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ABSTRACT

This paper examines the proposition that the business cycle affects seasonality in

industrial production, with output being switched to the traditionally low production

summer months when recent (annual) growth has been strong. This is investigated

through the use of a restricted threshold autoregressive model for the monthly growth

rate in a total of 74 industries in 16 OECD countries. Approximately one third of the

series exhibit significant nonlinearity, with this nonlinearity predominantly associated

with changes in the seasonal pattern. Estimates show that the summer slowdown in

many European countries is substantially reduced in the regime of higher recent growth.

JEL Classifications: E32, C22

KEYWORDS: Business cycles, seasonality, TAR models, industrial production

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1. INTRODUCTION

Economists and statisticians have traditionally viewed seasonal patterns as devoid of economic information, leading to the widespread use of seasonally adjusted data for the analysis of economic phenomena. Recently, however, this has been questioned by a number of authors. Studying various series, Ghysels (1993, 1994), Canova and Ghysels (1994), Cecchetti and Kashyap (1996), Miron and Beaulieu (1996), Cecchetti, Kashyap and Wilcox (1997), Carpenter and Levy (1998), Krane and Wascher (1999) have found evidence that seasonality changes over the business cycle. On the other hand, while agreeing that seasonality is not constant over time, van Dijk, Strikholm and Teräsvirta (2003) conclude that cyclical changes in seasonality for industrial production are relatively unimportant compared with changes in the seasonal pattern that depend on time alone.

It has been well documented that industrial production exhibits very strong seasonal movements, with developed countries in the Northern Hemisphere exhibiting marked declines in the summer and, to a lesser extent, around Christmas; see, for example, Miron and Beaulieu (1996). Presumably due to institutional and possibly climatic factors, the strength of this seasonality differs across countries. Nevertheless, the seasonal slowdown in production in certain months intuitively implies that, even at a business cycle peak, capital may not be fully utilised throughout the year. Therefore, with capacity fixed in the short-run, increased demand may be met by utilising spare capacity in low production months. Another possibility is that, when demand is slack during a recession, it may be less costly for producers to lay off workers (permanently or temporarily) in summer months, when production is already relatively low and

holidays are taken by many workers, rather than at other times of the year¹. Both of these point to seasonality being less pronounced during booms than recessions. More precisely, as examined in further detail by Cecchetti and Kashyap (1996), the effect of the business cycle on seasonality in production will depend on the properties of the marginal cost function and the costs of holding inventories.

The seasonal behaviour of inventories over the business cycle has been examined by Carpenter and Levy (1998) and Cecchetti et al. (1997). However, at least to date, the study of inventories in this context does not appear to offer substantial new insights compared with examination of output series. Using monthly production data for 11 industries in 19 countries, Cecchetti and Kashyap (1996) examine the seasonality/business cycle interactions by measuring the extent of seasonal variation near business cycle peaks compared with troughs, concluding that seasonality is generally less marked at peaks. Nevertheless, although their model is nonlinear, their approach is not entirely satisfactory because they effectively eliminate the nonlinearity by using a second-order approximation. They also take the business cycle indicator as given by an economy-wide variable after the application of the filter proposed by Baxter and King (1999), thereby utilising future information not available when production decisions are taken and also not focusing on the position within a specific industry. The approach of van Dijk et al. (2003) is more coherent, since they explicitly examine a nonlinear model that allows seasonal dummy variable coefficients to change as a function of the (lagged) change in the annual growth of the variable of interest. In fact, however, the model allows all parameters to vary over time as well as over the business cycle, leading to a highly parameterised specification.

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We are grateful to the referee who pointed out this possibility.

The results of van Dijk *et al.* (2003), implying that any interactions are relatively minor, have (in effect) questioned the findings of Cecchetti and Kashyap (1996) about the interactions between seasonality and the business cycle. We agree with Cecchetti and Kashyap that the existence, or otherwise, of interactions is important from an economic perspective because of the additional information this may provide about the nature of the cost function faced by producers. This paper sheds further light on the issue.

In terms of technique, our approach is fairly close to van Dijk *et al.* (2003). However, while they use quarterly aggregate industrial production for the G7 countries, we examine a potentially richer dataset of monthly industrial production series for 16 OECD countries, using data on major components as well as the aggregate. Thus we allow the possibility that different sectors may exhibit different business cycles. Further, the use of monthly data may be important because the effect of the dominant summer slowdown in production will be substantially masked at the quarterly level². We also provide a direct overall test for nonlinearity over the business cycle in a common framework for all series, while also allowing for deterministic time varying effects. In contrast, the tests of van Dijk *et al.* are indirect, in that they are based on Taylor series approximations to their underlying nonlinear model.

The outline of the paper is as follows. After discussion of the models in Section 2, the characteristics of our data, including the evidence for business cycle nonlinearities, are considered in Section 3. Estimates of the business cycle/seasonal interactions are then discussed in Section 4. However, to minimise problems associated with spurious effects, these results are considered only for those series that exhibit

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² Carpenter and Levy (1998) note that monthly inventory data reveals a large amount of seasonal variation that is undetectable with quarterly data.

(statistically) significant evidence of business cycle nonlinearity. Some conclusions (Section 5) complete the paper.

2. MODELLING SEASONAL/BUSINESS CYCLE INTERACTIONS

This study aims to test whether seasonality in production is associated with the business cycle and, where such interactions are found, to explicitly estimate the cyclical shifts in production over the twelve months of the year. In particular, we wish to examine the proposition that summer declines in production are less marked during business cycle expansions than recessions. The threshold autoregressive (TAR) approach is suitable for this purpose because it allows the parameters to change when growth exceeds some threshold. In order to focus explicitly on seasonality, we use a restricted form of the TAR model.

Our basic model is described in subsection 2.1, followed by a discussion of the practical issue of trending seasonality, which could be associated with technological and institutional changes, as considered by van Dijk *et al.* (2003). The section concludes with a discussion of estimation issues.

2.1 The Basic Model

The basic model we employ has the form

$$\phi(L)\Delta y_{t} = \delta_{0} + \gamma_{0}I_{t} + \sum_{j=1}^{11} \delta_{j}s_{jt} + \sum_{j=1}^{11} \gamma_{j}I_{t}s_{jt} + \varepsilon_{t}$$
(1)

where the disturbance process is $\varepsilon_t \sim NID(0, \sigma^2)$. The autoregressive operator $\phi(L)$, defined in terms of the usual lag operator L, is assumed to have all roots strictly outside the unit circle. Seasonality is captured through the variables s_{jt} which are defined by

 $s_{jt} = D_{jt} - D_{12t}$, j = 1, ..., 11 where D_{jt} are the conventional monthly seasonal dummy variables. This formulation is frequently used for seasonality because it allows the separation of the overall mean from the deterministic seasonal effects. More precisely, $\phi^{-1}(1)\delta_0$ is the overall steady state mean for Δy_t corresponding to the lower regime (with $I_t = I_{t-1} = ... = 0$).

In the lower regime at time t ($I_t = 0$), the coefficients δ_j (j = 1, ..., 11) measure the seasonal intercept shift in each of eleven months compared with the overall intercept δ_0 , with the intercept shift for the final month computed as $\delta_{12} = -\sum_{j=1}^{11} \delta_j$. The monthly seasonal deviations in steady state from the overall mean can be calculated from the parameters of (1), as discussed in Appendix II.

We define the regime indicator I_t by:

$$I_{t} = \begin{cases} 1 & \text{if } (1 + L + L^{2}) \Delta_{12} y_{t-1} \ge r \\ 0 & \text{if } (1 + L + L^{2}) \Delta_{12} y_{t-1} < r \end{cases}$$
 (2)

Equations (1) and (2) then define a restricted TAR model, where r is the (single) threshold parameter. The coefficients γ_j ($j=0,\ldots,12$) give the amount by which the overall intercept and seasonal intercept terms shift in the upper regime ($I_t=1$) compared with the lower, where the seasonal intercept shift omitted from (1) can be computed as $\gamma_{12}=-\sum_{j=1}^{11}\gamma_j$. Within the upper regime, the overall steady state mean is given by $\phi^{-1}(1)[\delta_0+\gamma_0]$, with the calculation of seasonal deviations from this mean again outlined in Appendix II.

From a behavioural perspective, (2) has the interpretation that seasonality changes when, over the previous three months, production has increased by more than some threshold amount r compared with a year earlier. For many countries, production peaks during the spring and early summer, before falling (sometimes dramatically)

during July or August; see, for example, the monthly growth rate patterns in Miron and Beaulieu (1996, Table 3). Therefore, it can be anticipated that capacity constraints will typically be more pressing in the spring and early summer than in other months of the year. The use of (2) as the business cycle indicator allows the possibility that the seasonal pattern in July/August will reflect conditions of capacity constraint (or, conversely, low demand) that have operated in these earlier months.

There are, of course, other possibilities than (2) for the definition of the regime. One possibility is to treat I_t as observed by using business cycle turning point dates to construct the regimes; for example, Canova and Ghysels (1994) adopt the NBER business cycle dates. However, these regimes are not known with certainty at the time that production decisions are made at t, so we prefer to use a more behavioural model that reflects available information. An obvious possibility is to use the lagged annual difference, $\Delta_{12}y_t$, without smoothing through the moving sum $1 + L + L^2$. However, some experiments with this specification indicated that it is too noisy as a business cycle regime indicator, implying relatively frequent regime changes. Another possibility is to define the regime in terms of differences over a period shorter than a year, allowing relatively quick reactions to business cycle regime changes. Seasonality in these shorter differences would imply the use of a seasonally varying threshold parameter, leading to a type of periodic TAR model. However, such models involve a large number of parameters and hence we prefer the more parsimonious specification of (2).

Note that, in contrast to the model used by van Dijk *et al.* (2003), (1) restricts changing seasonal behaviour to the seasonal intercepts, with no effect operating through the dynamics in $\phi(L)$. This restriction is adopted to keep the parameterisation as simple as possible, with the practical advantages that interpretation is straightforward and relatively few parameters need to be estimated. Nevertheless, we also believe that an

examination of shifts in the seasonal intercepts captures the essential feature of the possible relationship between seasonality and the business cycle. While we also acknowledge that omitting other possible sources of nonlinearity could bias the estimated nonlinear coefficients related to seasonality in our model, we attempt to guard against this by considering the economic plausibility of our results.

Another assumption implicit in this specification is that the series y_t is integrated of order 1, or I(1), when due allowance is made for deterministic seasonal effects through $\Sigma \delta_j s_{jt} + \Sigma \gamma_j s_{jt} I_t$. In particular, it is assumed that y_t contains no seasonal unit roots³. Indeed, the presence of seasonal unit roots would obscure the meaning of interactions between seasonality and the business cycle, because such roots imply that the seasonal pattern is subject to constant change and hence "summer can become winter"; see Ghysels and Osborn (2001). In any case, the existence of the full set of seasonal unit roots required for annual differencing appears to be relatively rare in practice; see, for example, Beaulieu and Miron (1993), Osborn, Heravi and Birchenhall (1999), van Dijk *et al.* (2003). Nevertheless, we acknowledge the potential importance of deterministic changes in the seasonal pattern over time, as discussed next.

2.2 Trending Seasonality

Equation (1) assumes that seasonality in Δy_t has constant mean over time, after allowing for cyclical changes. In practice, however, some of our industrial production series exhibit graphical evidence that the seasonal pattern is, at least for some months of the year, trending over time. Canova and Ghysels (1994) note the presence of such seasonal trends in M1, while they also appear to be a feature of inventory investment series examined by Carpenter and Levy (1998). Nevertheless, the models used in these

and other studies (including Cecchetti and Kashyap, 1996) do not incorporate trending seasonality. An exception is van Dijk *et al.* (2003), who model changing seasonality as logistic time trends. They find that trending seasonal effects dominate those associated with the business cycle, calling into question other results that do not allow for possible trends in seasonality over time.

Our approach to trending seasonality is to add a set of linear seasonal trends to (1). We guard against the possibility of a trend for Δy_t by also including an overall (nonseasonal) trend⁴. Thus, the model becomes

$$\phi(L)\Delta y_{t} = \delta_{0} + \lambda_{0}t + \gamma_{0}I_{t} + \sum_{i=1}^{11} \delta_{j}s_{jt} + \sum_{i=1}^{11} \lambda_{j}s_{jt}t + \sum_{i=1}^{11} \gamma_{j}I_{t}s_{jt} + \varepsilon_{t}$$
(3)

with $\varepsilon_t \sim NID(0, \sigma^2)$. There is one further complication. Equation (3) allows the possibility of an overall (nonseasonal) trend in Δy_t , while the presence of such a trend would imply that the threshold variable will also display trending behaviour. Since we wish to focus on business cycle behaviour, we avoid the possibility that I_t may be influenced by any change in the underlying growth rate by prior detrending. More specifically, we detrend the annual change employed in (2), using a prior regression on a constant and a linear time trend.

2.3 Estimation

Estimation of (3) can be undertaken using the standard approaches developed for TAR models. The crucial parameter is the threshold r, since ordinary least squares (OLS) can be applied conditional on its value. Chan (1993) shows that, for a given order of $\phi(L)$, searching over all possible values of r to minimise the sum of squared

³ There is no conflict between the assumption of no seasonal unit roots for y_t and the use of the annual difference $\Delta_{12}y_t$ in (2), since the latter is not modelled explicitly and is adopted only as a business cycle indicator.

⁴ It might be noted that this allows the possibility that y_t exhibits an underlying nonlinear (quadratic) trend.

residuals produces a super-consistent estimate of this threshold. To implement this search procedure, we chose an autoregressive order of 24, thereby allowing for dynamics of up to two years⁵.

Following conventional practice, for instance, Hansen (1996) or Tsay (1989), we apply the grid search for r over the empirical distribution of the threshold variable, excluding its extremes. Chan and Cheung (1994) argue that a natural way to robustify the estimate of the threshold parameter in TAR models is to restrict the interval over which the grid search is conducted, and thereby avoid the problem that one "regime" may correspond to only a small number of observations. This is particularly important in our context, since a reasonable number of observations in each regime are required in order to obtain reliable estimates of the regime-dependent monthly seasonal coefficients δ_j and γ_j in (3). Our specific procedure is to obtain the empirical distribution function of the threshold variable and to ignore the extreme 20 percent in both tails. The estimated threshold is then obtained by searching over the central 60 percent of the empirical distribution function in 1 percent increments. Conditional on this r, we then estimate (3) by OLS.

3. DATA CHARACTERISTICS

We analyse seasonally unadjusted monthly indexes of industrial production for 16 OECD countries available from the OECD *Main Economic Indicators* database. The variables and countries selected are those classified as industrial production series for the specific country and available over a long period. In all, 74 series are analysed.

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⁵ This relatively conservative value is selected in preference to choosing the lag order by an information criterion as part of the model selection procedure. Given the large number of series in our study, we prefer this on grounds of practicality. It also avoids some of the potential pitfalls of using an information

Information about the sample period and some descriptive statistics for each series can be found in Appendix I. It is clear that these variables represent a variety of historical experiences, as captured by their overall means and standard deviations. Typically, our series commence in January 1960, with the latest starting date used being January 1971. The sample ends in December 1994 or during 1995. Prior to analysis, all series are transformed to monthly percentage growth rates by taking first differences of the (natural) logarithms and multiplying by 100.

Both total industrial production (this being the monthly analogue of the series considered by van Dijk et al, 2003) and manufacturing output are available for all 16 countries studied here. In addition, for most countries, monthly industrial production data for the consumer goods (for either total or non-durable and durable separately), intermediate goods and investment goods sectors are also available. A small number of other series classified as industrial production are available for a few countries, the most common of these being the construction series included for four European countries. The countries covered include all G7 countries except Canada, which is omitted due to data availability considerations. European countries are covered particularly well, with 14 such countries represented. The two major non-European countries, namely the US and Japan, are included.

Virtually all series exhibit strong seasonality, as measured by the R^2 from a simple linear regression of the growth rate on twelve seasonal dummy variables; see Appendix I. Indeed, with the single exception of consumer goods in Greece, the value of this R^2 measure exceeds 0.5 for all 74 series. According to this measure, the extent of seasonality varies over countries, with the Scandinavian countries of Finland, Norway and Sweden having particularly marked patterns compared with, say, the US, UK or

criterion for lag selection in the context of seasonal time series; for example, Hall (1994) finds that such procedures may not work well when the autoregressive operator has a seasonal form.

Germany. This finding is not new. Indeed, when they examine the relative importance of country and industry effects in seasonal patterns for production series, Cecchetti and Kashyap (1996) conclude that the former dominate the latter.

Our model for seasonal/business cycle interactions has already been discussed in the previous section. However, inference in such models is not straightforward, because the key parameters capturing the interactions are not identified when the true process is linear. To guard against the possibility that the results obtained from the estimated models are spurious, prior testing for nonlinearity is undertaken. Other characteristics discussed in this section are outliers and the nature of the business cycle and the trend behaviour captured by the estimated TAR models.

3.1 Nonlinearity

The problem of how to conduct hypothesis tests is sometimes solved by linearisation of the nonlinear model. This is the route favoured by van Dijk *et al.* (2003) in their study of the interactions between seasonality and the business cycle for total industrial production. We, however, favour more direct tests based explicitly on our nonlinear TAR specification.

In the context of (3), linearity is tested through the null hypothesis

$$H_0: \gamma_0 = \gamma_1 = \gamma_2 = \dots = \gamma_{11} = 0$$
 (4)

A test of (4) involves non-standard inference, since the threshold parameter is not identified under the null hypothesis; this issue is discussed in detail by Hansen (1996). Hansen develops a testing procedure for such cases, using simulations to obtain the asymptotic distributions of test statistics produced by searching over a grid of values for the unidentified parameter(s). However, there is an important body of evidence suggesting that the use of an asymptotic approximation of this type is not entirely

satisfactory in the TAR and similar cases. Therefore, we opt for direct finite sample simulation, as described below⁶.

Using a grid search over r, as described above, (3) is estimated and the usual Wald F-test statistic for H_0 is computed. Since r is chosen to minimise the residual sum of squares, this Wald statistic must be the maximal value over the values of r considered and hence it is often denoted as sup-Wald. Monte Carlo simulations are then used to generate data from the estimated null (linear) model, and the TAR model estimation (including the grid search) is repeated for each of 10,000 replications in order to generate the empirical distribution of the test statistic under the null hypothesis⁷. The reported p-value for the sup-Wald statistic is obtained using this empirical distribution.

The summary *sup-Wald* test results in Table 1 (detailed results are in Appendix I), points to our nonlinear model being appropriate in some countries to a greater extent than in others. In particular, four out of five series for both Finland and Spain yield significant statistics at the 5 percent level, with two out of three series for Luxembourg also indicating significant business cycle nonlinearity. At the other extreme, none of the eight US series yield a significant *sup-Wald* statistic at even the 10 percent level. In terms of industrial sectors, this table also indicates that the aggregate industrial production and the manufacturing production series for around a quarter of the countries reject linearity. However, rejections are (proportionately) even more marked for the intermediate goods sector, with rejection for six of the nine series at 5 percent. Such nonlinearity is, however, apparently not an important general feature of the consumer

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⁶ Diebold and Chen (1996) provide an extensive study comparing the asymptotic and finite sample simulation approaches, in the related context of testing for structural change with unknown breakpoint. They find that the asymptotic procedure can show large size distortions in finite samples, while direct simulation results in an excellent approximation. In the TAR context, Potter (1995) also finds evidence of size distortions in a small Monte Carlo experiment of Hansen's procedure.

⁷ This number of replications should give a reasonable approximation of the true critical value for the *sup-Wald* statistic at significance levels of, say, 5% or greater. However, the smaller the empirical "*p*-value" reported, the less reliable is the approximation to the true *p*-value due to the smaller number of replications that allow estimation of the tail values of true *sup-Wald* distribution.

goods and investment goods sectors. Although pursuing the nature of the cost functions faced by firms is beyond the scope of the present paper, these result nevertheless suggest that firms in different countries and, perhaps, in different sectors within the same country, may face distinct cost functions.

TABLE 1 ABOUT HERE

In addition to the *sup-Wald* test, we also report results from the TAR nonlinearity test proposed by Tsay (1989); the implementation of this test is discussed in Appendix I. Overall, the Tsay test confirms the extent of nonlinearity found for our series, which is reassuring. There is some disagreement about the significance of nonlinearity for specific series. However, this is not surprising given the different forms of the tests and their different alternative hypotheses. More specifically, *sup-Wald* explicitly tests linearity against nonlinearity of the single threshold form of (3), whereas the Tsay (1989) test allows a more general form of nonlinearity under the alternative. As we wish to investigate seasonal/business cycle interactions in terms of the two-regime TAR model of (3), we anticipate the more specific *sup-Wald* statistic will have greater power and we pursue the analysis on the basis of significance of the *sup-Wald* statistic. Estimation results are presented in Table 2 for the series which yield a significant statistic at the 10 percent level.

TABLE 2 ABOUT HERE

3.2 Outliers

Conventional residual diagnostic tests for autocorrelation, ARCH effects and non-normality were computed for all estimated models of Table 2. In practice, these revealed no major problems, with the exception of excess kurtosis. Such excess kurtosis may be associated with outliers, which are known to be potentially important for the estimation of nonlinear models (see, in the context of smooth transition models, the discussions in Öcal and Osborn, 2000, or van Dijk, Franses and Lucas, 1999). For those series with significant excess kurtosis at the 1 percent level, dummy variables were introduced to handle outliers. Our procedure was to include a dummy for a specific observation when the largest residual (in absolute value) exceeded four times the overall residual standard deviation. The threshold variable (2) was corrected for the outlier by simple interpolation of the offending observation based on an AR(24) model for Δy_t , including seasonal dummy variables. The TAR model was then re-estimated and the procedure repeated until no further outliers were detected.

The detailed estimation results presented are computed with outlier dummies included and the number of such dummies is indicated⁸. As seen from Table 2, most series required none or only one outlier dummy.

3.3 Business cycle and trend characteristics

In addition to the *sup-Wald p*-value, Table 2 shows the *p*-value for a conventional *F*-test of the upper regime seasonal restrictions $\gamma_j = 0, j = 1, ..., 11$, which we denote F_{II} . Significance for individual coefficients, including the overall intercept shift term γ_0 , is indicated using conventional *t*-tests. Chan (1993) shows, in the context of a conventional TAR model, that estimation of the threshold parameter r is super-

consistent and hence, conditional on the presence of TAR nonlinearity, standard distributional results apply for the coefficients. The threshold itself is shown as the proportion of observations estimated to fall in the lower regime, denoted r^* .

An interesting result from Table 2 is that a shift in the overall (nonseasonal) intercept does not appear to be the dominant source of nonlinearity. Only four of the 26 series produce an estimate of γ_0 which is significant at 5 percent. In contrast, the F_{II} -test for constant seasonal dummy variable coefficients fails to reject the null hypothesis (at 5 percent) for only one series. Therefore, it appears that the nonlinearity detected by the *sup-Wald* statistic is associated primarily with a change in the seasonal pattern (rather than the overall intercept) over regimes. This result may be due to the use of monthly data, which is dominated by seasonal fluctuations, and where cyclical characteristics are relatively less important than with quarterly data⁹.

The estimated values of γ_{θ} and r^* indicate that the model captures a variety of business cycle characteristics in our series. In approximately a third of the series in Table 2, γ_{θ} is positive and r^* less than 0.5. In such cases it is reasonable to associate the lower regime with recession and the upper one with expansion, even though this labelling may not be entirely accurate. Other cases (such as Finland Total¹⁰ or France Intermediate) have estimated r^* greater than 0.5 with positive γ_{θ} , so that the regimes appear to be associated with high growth versus low to moderate growth. However, yet other series (including Spain Intermediate and Sweden Manufacturing) produce negative estimates of γ_{θ} . Although this implies a lower overall growth rate in the upper regime compared with the lower one, it must be recalled that the regimes are defined in

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⁸ Our outlier procedure was invoked only for the series of Table 2, namely series that yielded a significant *sup-Wald* statistic (at 10 percent). Where relevant, the values presented for this statistic in Table 2 and the Appendix Table are computed for the model including outlier dummies.

⁹ We are grateful to a referee for this point.

terms of the annual growth rate over the previous three months, and not the contemporaneous growth rate.

Significant (at the 5 percent level) overall trend effects are indicated by the estimated λ_0 in Table 2 for eight series. In all these cases, the trend is downward. Therefore, although the mean growth is almost always positive over the sample period, in many cases it has nevertheless declined significantly over time. Perhaps more remarkable, however, is that the F_{II} -statistic that tests the presence of seasonal trends through the null hypothesis $\lambda_j = 0$, j = 1, ..., 11, points to these being significant at 5 percent for 18 of the 26 series. This echoes the important role found by van Dijk *et al.* (2003) for seasonal trends in aggregate quarterly industrial production series.

The next section examines the nature of the changes in seasonality over the regimes of the TAR model.

4. SEASONALITY OVER THE BUSINESS CYCLE

The results in Table 2 include the estimated seasonal dummy variable coefficients in the lower regime, the seasonal shift terms which apply for the upper regime and the estimated seasonal trend coefficients. That is, in terms of (3), we show the estimated values of δ_j , γ_j and λ_j (j=1,...,11), together with an indication of significance for each coefficient according to a conventional t-test. The twelfth (December) seasonal coefficient and its significance is obtained in each case from the restriction that the corresponding terms must sum to zero over the year.

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¹⁰ The recent contribution of Teräsvirta, Strikholm and van Dijk (2003), undertaken subsequent to the analysis of the present paper, also finds significant seasonal/business cycle interactions with this pattern for aggregate quarterly industrial production for Finland.

Our interest focuses on the seasonal/business cycle interactions and, in Figure 1, we also present the implied deviation in steady state for each month in relation to the overall mean. These mean deviations are shown for both the upper and lower regimes. The details of our computational method are presented in Appendix II, but it should be noted here that each seasonal mean deviation depends on all seasonal intercepts, with weights that are nonlinear functions of the autoregressive parameters. The series included in Figure 1 are identical to those in Table 2, namely those series that produce a significant *Sup-Wald* statistic at the 10 percent level. Figure 1 expresses the means as deviations from the overall mean in each regime, with the trend terms ignored, so that each set of monthly seasonal mean deviations sums to zero.

FIGURE 1 ABOUT HERE

Both the coefficients of Table 2 and the seasonal means of Figure 1 indicate that industrial production series of European countries typically experience their largest seasonal change in July or August, depending on the country, with a large fall immediately followed by an increase of similar magnitude in the following month. It is precisely this summer slowdown that exhibits the greatest effect from cyclical influences. To be specific, ignoring German Construction (which does not exhibit a marked summer slowdown) and the three Japanese series, 16 out of the remaining 22 series in Table 2 show the estimated upper regime shift coefficient corresponding to the summer slowdown, γ_7 or γ_8 as appropriate, to be positive and significant at the 5 percent level. The size of this estimated seasonal intercept shift is not negligible, as its magnitude is typically equal to one or two times the residual standard deviation. Corresponding to the reduced summer slowdown, the mean growth in the following one

or two months also tends to be lower in the upper regime, which is also compatible with the summer reduction being less dramatic. These results are consistent with the hypothesis of Cecchetti and Kashyap (1996) that firms reallocate production to the usually slack summer months during business cycle expansions. Conversely, the results are also consistent with worker layoffs and temporary production shutdowns taking place in summer during recession periods.

The one non-European country represented in Table 2 and Figure 1 is Japan. Although the summer slowdown is not as dominant as for European countries, the general pattern is again a summer decline that is tempered in the upper regime compared with the lower one.

There is also evidence in some series of a seasonal reallocation of production in the upper regime at the Christmas holiday period (December and/or January), although it is not as large or widespread as the cyclical change observed during the summer. For example, Figure 1 shows that the mean for the Austrian Intermediate series exhibits a substantial seasonal fall in December, with this being less dramatic in the upper than the lower regime.

There are some notable exceptions to the comments just made. In particular, the construction industry in various countries exhibits a pattern where a December/January decline is exaggerated in the upper regime compared with the lower. This pattern is particularly notable in Figure 1 for German Construction. The four countries for which we have data on the construction industry are France, Germany, Belgium and Luxembourg, and these may have substantial winter seasonal effects. Note that Table 2 shows significant negative upper regime shift coefficients for the winter months (December, January and/or February, depending on the country) for these construction series. It is possible that this additional seasonality detected during winter in the upper

regime may relate to the weather, rather than a conscious choice to reallocate production over months. Consider the situation where output has been growing strongly in the autumn, leading to a high level in December say, but only a given level of construction activity is feasible in January because of the weather. In this case, a *greater* decline will result compared with the norm. Unfortunately, we do not have data for construction series in the Scandinavian countries, which would provide further information on possible weather effects.

Because we have used significance of the business cycle effects as the criterion for inclusion in Figure 1 (and Table 2), not all countries are examined there. However, there do appear to be substantial country-specific influences that affect the extent of interaction between seasonal patterns and the business cycle. In particular, the reduction of the summer slowdown in the upper regime appears to be less pronounced for Austria, Germany, Japan and the UK than for other included countries.

Although our interest focuses on the seasonal/business cycle interaction, it might be noted from Table 2 that significant seasonal trend terms are often observed in the summer months. Focusing again on the month with the largest summer reduction, namely July or August as appropriate, the associated trend coefficient is typically negative and significant (this is the case at 5 percent in 15 of the 26 cases). Therefore, over time the summer reduction has generally increased in magnitude. Nevertheless, the opposite is true for the two UK series, and also Germany Food and Norway Manufacturing, where the magnitude of the summer seasonal is reduced over time. A significant increase in the December seasonal slowdown is noticeable in many cases, with a negative trend combining with a negative seasonal intercept. Since all series, with the single exception of Belgium Construction, have positive mean growth over our sample period (see the table of Appendix I), the phenomenon of reduced seasonality in

the upper business cycle regime appears to be a short-term one. The evidence from the seasonal trend terms suggests that, in the longer term, capacity generally expands with production to facilitate the seasonal pattern in production, or even to allow the magnitude of this seasonal pattern to increase over time.

5. CONCLUSIONS

We have found evidence of business cycle nonlinearity in around a third of the monthly industrial production series examined. To summarise our substantive finding, production is spread more smoothly over the months of the year when the series is growing strongly than when it is not. In particular, the summer slowdown is less marked when recent growth has been relatively strong. Although we use a different approach, our findings reinforce those of Cecchetti and Kashyap (1996) relating to seasonal patterns in production, and also those of other authors (including Ghysels, 1993, 1994, Canova and Ghysels, 1994, Miron and Beaulieu, 1996, Cecchetti, Kashyap and Wilcox, 1997, Carpenter and Levy, 1998, Krane and Wascher, 1999) who document interactions between seasonality and the business cycle.

Our results also raise some interesting issues. Although we define business cycle regimes in terms of the (lagged) annual growth rate, the regimes appear to exhibit greater effects on the seasonal pattern than on the overall series mean. In other words, the stage of the business cycle captured here generally has more impact on the organisation of production over the months of the year than on the overall growth rate of output. From the work of Cecchetti and Kashyap (1996), this may reflect the cost structures in different industries and countries. Although it may be difficult to separate

cyclical and seasonal movements in monthly data, our results imply that the use of seasonally adjusted data will effectively obliterate any information in seasonality about the stage of the business cycle.

Seasonal/business cycle interactions are apparently stronger in some countries than others. Indeed, although much earlier work focuses on the US, the interactions there appear to be substantially weaker than in European countries such as Finland, Germany and Spain. Further, the communality of some patterns across series within such countries in Figure 1 points to the potential value of a panel data approach. This is, however, beyond the scope of the present paper.

We find an important aspect of seasonality in industrial production to be the trend-like changes in the pattern that have occurred over our sample period. If the explanation of changing seasonality over the business cycle lies in the nature of the cost function faced by producers, then we might anticipate that at least part of these seasonal trends may also be attributable to similar causes. Research may be warranted on whether long-run changes to the seasonal pattern in production shed further light on the nature of the cost function faced by producers.

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Table 1. Summary Nonlinearity Test Results

	Series	Signific	ant at		Series	Signifi	cant at
Country	#	5%	10%	Classification	#	5%	10%
Austria	5	1	1	Total industrial prod.	16	4	4
Belgium	7	0	1	Manufacturing	16	3	6
Finland	5	4	4	Consumer durables	3	0	1
France	7	1	2	Consumer non-durables	3	0	0
Germany	7	1	3	Consumer goods	9	1	2
Greece	4	0	0	Intermediate goods	9	6	6
Italy	4	1	2	Investment goods	11	2	2
Japan	6	1	3	Construction	4	2	4
Luxembourg	3	2	2	Other series	3	0	1
Nederlands	2	0	0				
Norway	2	1	1				
Portugal	2	0	0				
Spain	5	4	4				
Sweden	2	0	1				
United Kingdom	5	2	2				
United States	8	0	0				
Total	74	18	26		74	18	26
Percentage		24%	35%			24%	35%

Table 2. Estimated Models

						Estimat	ted Coeffi	cients							SupWald	σ
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	γ_0/λ_0	F_{II}	r*	Outliers
Austria Intermediate													•			
Lower regime	-8.91 a	0.91	5.60 a	5.95 a	3.41	-0.06	-9.60 a	-8.26 a	7.46 a	6.70 a	4.0 7 b	-7.25 a				
Upper regime shift	2.68 b	-1.47	-3.51 a	-1.06	-0.47	-0.14	0.55	0.21	1.02	-0.93	-0.69	3.83 a	0.53	0.003	0.023	3.18
Trend	-0.018 a	-0.007	0.002	0.006	0.002	0.000	-0.008	-0.035 a	0.019 a	0.021 a	0.002	0.016 b	0.000	0.000	0.50	0
Belgium Construction																
Lower regime	14.57	-8.79	16.22 b	8.18	1.26	<i>17.56</i> b		<i>35.03</i> ^a	11.15	-1.86	1.07	-33.48 a				
Upper regime shift	-22.87 a	1.87	<i>-13.71</i> b	1.38	4.03	1.04	<i>13.22</i> b	-6.86	3.27	3.16	4.85	10.61	-1.65	0.006	0.061	15.04
Trend	0.046	0.001	-0.010	-0.006	-0.008	0.041	-0.102 a	0.049	0.028	-0.003	-0.001	-0.033	-0.006	0.070	0.28	0
Finland Intermediate																
Lower regime	1.85	0.24	4.69	0.30	-2.77	-2.18	<i>-21.15</i> ^a	10.09 a	7.52 a	4.05	0.58	-3.21				
Upper regime shift	1.50	-0.95	-1.92	-1.60	0.84	0.26	7.72 a	<i>-3.51</i> b	-1.96	0.50	0.18	-1.06	0.39	0.001	0.021	3.84
Trend	-0.003	0.003	-0.005	0.011	-0.002	0.019 a	-0.017 a	-0.006	0.004	-0.009	0.006	-0.003	-0.002	0.069	0.21	3
Finland Investment									1							
Lower regime	0.42	4.83	3.13	-6.11	0.17	-3.63	-41.93 a	10.72	13.55 b		0.83	-1.00				
Upper regime shift	-0.20	1.49	0.19	1.95	-2.29	1.17	11.51 ^a	-4.81 b	-2.20	<i>-4.03</i>	-1.42	-1.35	2.41 b	0.000	0.000	6.29
Trend	-0.030 a	-0.008	-0.008	0.019	0.019	0.016	-0.013	-0.004	-0.003	0.001	0.001	0.010	0.000	0.131	0.38	11
Finland Manufacturing										h						
Lower regime	1.58	-1.87	0.41	3.84	1.25	-4.82	-18.47 a	8.12 a	4.84	5.89 b	-0.86	0.08				
Upper regime shift	-0.64	1.22	<i>3.50</i> b	-1.71	1.72	-2.94 b		<i>-3.58</i> b	-2.28	-1.99	-0.25	0.59	0.91	0.000	0.000	3.62
Trend	-0.005	-0.002	0.003	-0.003	0.006	0.005	-0.001	0.002	0.004	0.004	-0.004	-0.009	-0.002	0.818	0.80	3
Finland Total								. h	h							
Lower regime	0.92	0.49	1.39	1.01	0.18	-3.51	-12.32 a	5.68 b	4.44 b	3.57	-0.65	-1.21				
Upper regime shift	0.07	0.38	0.50	0.51	1.30	-1.88	6.86 a	-3.15 b	-3.01 b		-0.64	0.73	0.88	0.000	0.000	2.86
Trend	-0.003	-0.002	0.002	-0.001	0.004	0.006	-0.001	-0.001	0.002	0.002	-0.001	-0.007	-0.002	0.915	0.80	0
France Construction				b	h							h				
Lower regime	-2.70	-0.00	1.47	9.39 b	8.69 b	5.18	-4.86	<i>-31.04</i> a	14.28 a	6.63	1.58	-8.63 b				
Upper regime shift	-4.40 a	-3.88 b		-1.21	-0.43	2.00	2.13	2.47	0.84	1.31	-0.11	1.72	1.65	0.025	0.087	5.31
Trend	0.030 a	0.018	-0.005	-0.002	0.016	0.000	-0.017	-0.052 a	0.013	0.004	0.010	-0.014	-0.005	0.001	0.40	0
France Intermediate	10.00	0.01	7 04		∡o = = h		10.003	42 (03	22.073	4.0=	0.07	40 c≖ h				
Lower regime	13.06	-0.01	5.81	-7.14	10.75 b	-2.14	-13.23 a	-43.60 a	33.87 a	4.07	9.25	-10.67 b	0.04	0.022	0.000	2.22
Upper regime shift	-0.29	-0.51	-0.52	-0.18	-1.65	-1.32	-1.05	4.75 a	-3.43 b		1.45	2.20	0.94	0.032	0.000	3.33
Trend	0.023 a	-0.001	<i>0.017</i> b	-0.006	0.019 a	0.005	0.027 a	-0.021 a	0.004	-0.017 b	-0.009	-0.039 a	-0.004 b	0.000	0.67	4

Table 2 (continued)

Tuble 2 (continueu)						Estimat	ed Coeffi	cients							SupWald	σ
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	γ_0/λ_0	F_{II}	r*	Outliers
Germany Construction													-			
Lower regime	-11.17 ^a	-7.86 b	13.62 a	8.46 b	4.63	7.06	2.71	-1.41	7.34 b	0.57	-5.41	-18.54 a				
Upper regime shift	-11.30 a	8.03 b	-4.34	-3.80	-1.76	-2.48	2.13	1.73	1.44	1.05	6.54 b	2.77	1.30	0.005	0.048	8.64
Trend	0.051 a	-0.044 a	0.043 a	-0.007	-0.017	0.000	0.017	-0.006	0.003	0.009	-0.014	-0.034 b	0.000	0.001	0.58	2
Germany Food																
Lower regime	-7.49 a	-5.18 a	2.93	5.37 a	1.10	0.85	-5.3 7 ^a	-3.68 b	1.93	6.80 a	6.88 a	-4.16 a				
Upper regime shift	-0.32	-0.62	-1.32	-1.73	2.18 b	-0.52	-0.58	1.11	-0.46	2.62 b	0.81	-1.16	-1.15 a	0.122	0.096	2.71
Trend	0.031 a	-0.001	0.026 a	-0.031 a	-0.016 b	-0.019 a	0.017 b	0.031 a	0.006	0.008	-0.010	-0.043 a	-0.002	0.000	0.26	1
Germany Manufacturin																
Lower regime	-5.92 a	0.49	6.14 a	1.28	<i>-3.31</i> b	0.20	-1.26	-7.81 ^a	6.01 a	6.39 a	2.42	-4.64 a				
Upper regime shift	1.68	-0.66	-1.94 b	-0.56	0.16	1.99 b	-1.29	-0.68	-1.32	0.11	0.34	2.18 b	1.05 b		0.091	2.65
Trend	0.011 b	-0.001	0.018 a	-0.016 a	-0.018 a	-0.007	0.027 a	0.007	-0.007	0.011	-0.007	-0.019 a	-0.003 b	0.000	0.55	1
Italy Consumer																
Lower regime	<i>13.24</i> b	-2.33	-4.49	18.78 a	7.07	-11.65	8.26	-48. 74 ^a	21.49 a	-7.30	-9.19	0.44				
Upper regime shift	-1.14	0.47	0.48	-2.67	-1.87	1.09	-1.03	5.43 a	-1.36	-2.31	0.20	2.73	1.68	0.030	0.094	4.15
Trend	0.021	0.008	0.014	0.000	0.009	0.012	-0.005	-0.073 a	0.009	-0.005	-0.004	0.013	-0.004	0.031	0.62	0
<u>Italy Total</u>																
Lower regime	2.47	5.49	3.84	5.53	-1.09	-0.07	-3.95	-38.58 a	19.67 ^a	5.64	<i>7.33</i>	-6.29				
Upper regime shift	-2.53 b	<i>-2.75</i> b	1.54	-0.14	-0.23	0.09	0.01	4.69 a	-3.09 b	-0.59	0.23	2.75 b	1.00	0.000	0.006	3.34
Trend	0.004	0.014	0.014	0.010	-0.008	0.001	0.000	-0.088 a	0.039 a	0.013	0.019	-0.018	-0.005 a	0.000	0.33	1
Japan Consumer Durab		,							,							
Lower regime	-10.03 a	6.01 b	8.33 a	-1.75	-6.15 a	8.53 a	6.59 a		6.36 b	9.11 a	-3.21	-4.48				
Upper regime shift	-3.44 a	-0.12	-1.25	1.56	1.61	-1.49	<i>-2.27</i> ^b	0.78	-0.76	1.60	<i>2.70</i> b	1.06	-0.36	0.010	0.059	2.94
Trend	0.023 a	0.010	0.015 b	-0.021 a	-0.012	0.006	0.023 a	-0.049 a	0.020 a	0.017 b	0.004	-0.036 a	-0.005 b	0.000	0.29	1
Japan Intermediate					,				,							
Lower regime	-7.59 a	-0.05	7.02 a	2.13	<i>-2.25</i> b	<i>3.70</i> ^a	1.21	-7.98 ^a	<i>2.79</i> b	3.91 a	-1.96	-0.94	,			
Upper regimeshift	0.77	-0.10	-0.64	-3.12 a	-0.15	-1.14	0.27	1.33 b	0.80	0.95	0.62	0.41	-0.61 b	0.006	0.054	1.38
Trend	0.000	0.004	0.005	0.002	-0.009 a	0.007 a	0.008 a	-0.018 a	0.005	0.007 b	-0.001	-0.009 a	-0.001	0.000	0.21	3
Japan Manufacturing																
Lower regime	-3.99 a	-0.19	8.57 a	-1.79	-5.3 7 ^a	3.98 a	4.16 a	-8.82 a	4.80	2.24	-5.13 a	1.55				
Upper regime shift	-0.68	-0.99	<i>-1.22</i> b	0.94	0.09	-0.80	-0.93	0.28	-0.23	1.97 a	0.69	0.88	-0.07	0.001	0.030	1.44
Trend	0.000	-0.001	0.006	0.005	-0.013 a	0.005	0.016 a	-0.021 a	0.008 b	0.006	-0.004	-0.008 b	-0.002 b	0.000	0.27	2

Table 2 (continued)

ruore 2 (continueu)						Estimat	ted Coeffi	cients_							SupWald	σ
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	γ_0/λ_0	F_{II}	r*	Outliers
Luxembourg Construct	tion															
Lower regime	-5.65	-13.01	7.04	3.53	11.96	3.52	4.63	<i>-25.30</i> a	2.18	1.21	6.75	3.14				
Upper regime shift	-21.08 a	5.87	0.42	5.37	3.02	7.37	4.65	2.52	5.73	2.72	-3.88	<i>-12.72</i> b	-2.38	0.005	0.050	12.31
Trend	0.022	0.030	0.022	-0.025	-0.008	-0.005	0.021	-0.184 ^a	0.052	0.012	0.046	0.017	0.004	0.000	0.23	1
Luxembourg Total																
Lower regime	-3.78	3.30	2.50	4. 73 ^b	0.17	3.00	-4.52 b	-18.00 a	1.79	7.69 a	-3.22	0.23				
Upper regime shift	2.99	-0.02	-0.63	0.12	-1.63	-3.50 b	0.54	5.71 a	<i>-3.72</i> b	1.63	-1.52	0.01	0.35	0.001	0.021	4.31
Trend	-0.004	0.008	0.003	0.008	-0.015	0.004	-0.006	-0.046 a	0.015	0.017	0.024 a	-0.009	0.000	0.000	0.45	3
Norway Manufacturing	2															
Lower regime	-3.65	6.27	6.12	14.78 a	-2.67	<i>12.00</i> b		-7.15	9.01	10.99 b	<i>12.00</i> b	-7.04				
Upper regime shift	0.17	-0.39	-1.81	-2.02	0.24	-1.42	6.46 a	0.40	-2.33	-0.49	0.27	0.91	0.73	0.000	0.027	3.91
Trend	0.009	0.003	-0.004	-0.002	0.000	-0.001	0.009 b	0.003	-0.001	-0.007	-0.005	-0.007	-0.003 b	0.408	0.37	2
Spain Consumer																
Lower regime	1.98	6.48	5.52	3.45	2.67	-6.56	2.15	-35.66 a	19.96 a	11.18 a	-0.59	-10.59 b				
Upper regime shift	3.99 b	-0.14	-1.61	-2.02	0.17	1.90	-1.81	5.40 a	-5.28 a	-4.03 b	2.16	1.27	0.33	0.003	0.017	4.09
Trend	-0.001	0.007	0.003	-0.014	0.010	-0.005	0.020	-0.063 a	0.049 a	0.029 b	0.007	-0.042 a	-0.008 b	0.000	0.26	0
Spain Intermediate																
Lower regime	3.06	-1.45	1.29	-0.18	0.54	-1.79	-0.08	-17.19 a	7.61 a	7.71 ^a	1.87	-1.40				
Upper regime shift	-0.15	0.66	1.16	-0.08	-0.17	1.63	-1.10	5.57 a	-2.91	-2.9 7 b	-1.33	-0.32	<i>-1.07</i>	0.021	0.020	0
Trend	0.014	0.002	0.002	-0.007	0.011	-0.001	0.016	-0.044 a	0.017	0.002	0.002	-0.015	-0.004	0.116	0.75	3.28
Spain Investment																
Lower regime	11.68	-3.14	9.15	8.00	0.28	-7.46	-5.98	-48.28 a	10.66	17.74 a	1.87	-1.40				
Upper regime shift	-4.20	7.39	1.52	0.65	2.05	3.92	-5.87	19.37 a		-10.91 b	-4.18	1.56	-1.29	0.000	0.025	9.21
Trend	0.043	0.008	0.027	0.010	-0.012	-0.037	-0.028	-0.069 b	0.004	0.033	0.012	0.009	0.001	0.196	0.68	3
Spain Manufacturing												_				
Lower regime	2.52	3.45	6.12	1.89	3.44	-6.33	0.49	<i>-32.41</i> ^a	15.21 a	14.13 ^a	0.85	-9.36 b				
Upper regime shift	2.26	-0.64	-0.89	-1.81	0.55	1.47	-1.48	6.48 a	-5.72 a	-2.89	0.37	2.31	-0.10	0.002	0.045	3.66
Trend	0.015	0.007	0.012	-0.012	0.016	-0.011	0.020	-0.083 a	0.034 b	0.038 a	0.003	-0.038 a	-0.006 b	0.000	0.21	0
Sweden Manufacturing	<u> </u>															
Lower regime	-1.67	-0.55	-3.07	-2.97	2.60	-3.55	-13.56 a	5.70	5.9 7	5.19	5.72	0.18				
Upper regime shift	2.58	1.46	2.65	0.81	-3.56 b		-0.32	-5.09 a	-0.37	-2.79	1.88	2.80	-1.05	0.043	0.061	3.88
Trend	-0.009	-0.003	0.004	0.000	0.001	0.004	0.022 a	-0.012 b	0.000	-0.005	-0.001	-0.001	0.000	0.037	0.78	3

Table 2 (continued)

						Estimat	ted Coeffi	cients							supWald	σ
	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	γ_0/λ_0	F_{II}	r*	Outliers
UK Intermediate																
Lower regime	3.81	0.31	5.00	-5.27 b	-5.28 a	-2.47	-5.22 a	-10.60 a	8.41 a	9.23 a	6.26 a	-4.19 b				
Upper regime shift	-1.80	-2.37	-1.23	-5.69 a	0.50	0.40	1.46	3.44 b	1.76	0.23	1.50	1.80	0.99	0.004	0.029	2.97
Trend	0.009	-0.007	0.015 b	-0.006	-0.008	-0.006	0.019 b	0.017 b	-0.019 b	-0.008	0.004	-0.009	0.001	0.011	0.40	0
UK Total																
Lower regime	-0.19	-0.85	5.24 a	-1.58	-5.10 a	-1.18	-3.82	-9.0 7 ^a	7.96 a	7.72 a	4.14 b	-3.27				
Upper regime shift	-0.07	0.47	-0.86	-2.45 a	-0.87	0.13	-0.22	1.98 b	0.41	-0.46	1.21	0.73	-0.21	0.002	0.038	2.49
Trend	-0.002	-0.011 b	0.012 a	-0.005	-0.008	0.000	0.015 a	0.011 a	-0.007	-0.001	0.000	-0.004	-0.001	0.000	0.29	3

The columns labelled Jan-Dec show the estimated coefficients for the seasonal intercepts in the lower regime (δ_j) , the shift terms corresponding to the upper regime (γ_j) , and the coefficients for the seasonal trends (λ_j) ; γ_0 is the coefficient for the shift in the nonseasonal intercept in the upper regime and λ_0 is the overall trend coefficient; F_{II} is the p-value for the conventional F-test of $\gamma_j = 0$ or $\lambda_j = 0$ o

Bold numbers : p-value ≤ 0.10

^b 0.01 < p-value ≤ 0.05

^a p-value ≤ 0.01

APPENDIX I

Descriptive Statistics and Nonlinearity Test Results: All Series

The Appendix Table below reports descriptive statistics for all series: sample period, mean, standard deviation and R^2 from a regression on twelve seasonal dummies. Also shown are the regime for the estimated TAR model of equation (3). former, the threshold estimate is shown as r^* , results (as p-values) for the Sup-Wald and Tsay nonlinearity tests discussed in Section 3.1. For the *, which is the proportion of observations in the lower

conventional F-distribution. using recursive residuals obtained after all variables are re-ordered according to the threshold variable of (2). Tsay shows that, for large samples, the associated F-statistic follows the autoregression again taken to be 24. The test is based on a conventional F-test statistic computed regime. The basis of Tsay's test in our context is a k-regime TAR model, with the order of each under the alternative all the coefficients (intercepts, trend and autoregressive) may change with the the alternative hypothesis. Also, no particular form of the nonlinearity is assumed in the sense that The Tsay (1989) test is general in that no specific number of thresholds is assumed under

significant *p*-value of the two *F*-tests obtained in this fashion. missed within this initial portion. generate the test with both increasing and decreasing orderings of the data so that no threshold is minimum number of observations. We choose 10 percent of the sample for this purpose and In practice, the recursive estimation using the re-ordered data begins from a certain The Tsay test result shown in the table below is the more

Appendix Table. Descriptive Statistics and Nonlinearity Test Results for All Series

Country	Series	Sampl	Sample period	Mean	Std.dev.	R^2	Sup- $Wald$	Tsay	r^*
Austria	Consumer	1960:01	1995:07	0.27	9.72	0.83	0.844	0.006	0.64
	Intermediate	1960:01	1995:07	0.31	7.25	0.66	0.023	0.004	0.50
	Investment	1960:01	1995:07	0.41	17.42	0.84	0.241	0.271	0.75
	Manufacturing	1960:01	1995:05	0.32	9.15	0.78	0.660	0.337	0.79
	Total	1960:01	1995:07	0.32	7.59	0.78	0.831	0.052	0.33
Belgium	Construction	1960:01	1994:12	-0.06	39.60	0.76	0.061	0.947	0.28
	Consumer Dur.	1960:01	1994:12	0.23	17.33	0.89	0.886	0.524	0.65
	Consumer Non-Dur.	1960:01	1994:12	0.16	9.06	0.77	0.877	0.564	0.80
	Intermediate	1960:01	1994:12	0.16	11.84	0.88	1.000	0.665	0.50
	Investment	1960:01	1994:12	0.21	14.43	0.76	0.289	0.239	0.21
	Manufacturing	1960:01	1994:12	0.21	12.18	0.88	0.987	0.483	0.50
•	Total	1960:01	1994:12	0.18	11.86	0.89	0.993	0.499	0.72
Finland	Consumer	1960:01	1995:07	0.22	19.27	0.91	0.914	0.564	0.80
	Intermediate	1960:01	1995:07	0.26	14.95	0.80	0.021	0.000	0.21
	Investment	1960:01	1995:07	0.38	31.24	0.91	0.000	0.421	0.38
	Manufacturing	1960:01	1995:07	0.26	19.48	0.92	0.000	0.000	0.80
	Total	1960:01	1995:07	0.27	17.38	0.93	0.000	0.000	0.80
France	Construction	1960:01	1995:06	0.15	19.54	0.85	0.087	0.000	0.40
	Consumer	1963:01	1995:06	0.30	25.69	0.93	0.794	0.337	0.73
	Energy	1963:01	1995:06	0.16	9.38	0.73	0.122	0.154	0.50
	Intermediate	1963:01	1995:06	0.18	21.75	0.97	0.000	0.030	0.67
	Investment	1963:01	1995:06	0.26	18.93	0.67	0.840	0.000	0.21
	Manufacturing	1960:01	1995:06	0.22	18.18	0.94	0.233	0.192	0.59
	Total	1960:01	1995:06	0.22	17.04	0.93	0.641	0.047	0.61

Appendix Table (continued)

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		Sample	Sample period		Std.dev.	O CO	Sup-Wald	Tsay	7 P
Оеппапу	Consumer	1960.01	1994.12	0.13	9.20	0.00	0.046	0.094	0.50
	Food	1960:01	1994:12	0.22	6.87	0.54	0.096	0.209	0.26
	Intermediate	1960:01	1994:12	0.21	5.69	0.66	0.228	0.149	0.25
	Investment	1960:01	1994:12	0.25	10.75 7 57	0.77	0.248	0.000	0.20
	Total	1960:01	1994:12	0.22	7.10	0.71	0.339	0.147	0.24
Greece	Consumer	1961:01	1995:05	0.39	8.05	0.47	0.746	0.000	0.75
	Investment	1961:01	1995:05	0.42	9.99	0.55	0.215	0.255	0.61
	Total	1962:01	1995:05	0.39	6 41 6 41	0.54	0.668	0.124	0.38 0.24
Italy	Consumer	1971:01	1995:05	0.24	33.81	0.95	0.094	0.080	0.62
	Investment	1971:01	1995:05	0.35	41.96	0.93	0.629	0.897	0.58
	Manufacturing Total	1960:01	1995:07	0.27	30.61 27.03	0.86	0.2/4	0.565	0.28
Japan	Consumer Dur.	1960:01	1995:08	0.56	10.63	0.82	0.059	0.213	0.29
	Consumer Non-Dur.	1960:01	1995:08	0.29	9.23	0.77	0.330	0.003	0.57
	Intermediate	1960:01	1995:08	0.41	4.58 11.28	0.83	0.054	0.000	0.22
	Manufacturing	1960:01	1995:08	0.44	6.62	0.87	0.030	0.005	0.27
	Total	1960:01	1995:08	0.44	6.34	0.87	0.370	0.000	0.22
Luxemb'g	Construction	1960:01 1960:01	1994:12 1995:06	0.00	35.38 11 37	0.53	0.050 0.275	0.167	0.23
	Total	1960:01	1995:06	0.20	10.98	0.65	0.021	0.004	0.45
Netherlands	Manufacturing	1960:01	1995:06	0.31	7.76	0.81	0.403	0.002	0.21
Norway	Consumer	1960.01	1991-12	0.26	18 62	0.73	0.104	0.052	0.41
	Export	1960:01	1991:12	0.58	14.65	0.71	0.216	0.091	0.54
	Intermediate	1961:01	1991:12	0.26	19.64	0.92	0.315	0.000	0.37
	Investment Manufacturing	1960:01	1991:12	0.30	34.60 25.44	0.8/	0.150 0.027	0.000	0.78
	Total	1960:01	1995:07	0.39	18.21	0.80	0.678	0.679	0.74
Portugal	Manufacturing	1960:01	1995:06	0.35	14.03 12.62	0.61	0.346	0.140	0.80
Spain	Consumer	1965:01	1995:06	0.37	19.82	0.87	0.017	0.183	0.26
-	Intermediate	1965:01	1995:06	0.30	14.86	0.79	0.020	0.074	0.75
	Investment	1965:01	1995:06	0.24	45.15	0.80	0.025	0.282	0.68
	Total	1961:01	1995:06	0.38	18.12	0.80	0.045	0.139 0.358	0.21
Sweden	Manufacturing Total	1960:01 1960:01	1995:07 1995:07	0.12	32.31 32.18	0.95 0.95	0.061 0.189	0.227 0.114	0.78 0.48
UK	Consumer	1968:01	1995:04	0.10	8.05	0.88	0.369	0.680	0.21
	Intermediate	1968:01	1995:07	0.11	7.36 10.95	0.75	0.029 0.737	0.115	0.40
	Manufacturing	1960:01	1995:07	0.11	8.29	0.76	0.254	0.375	0.22
	Total	1960:01	1995:07	0.13	7.42	0.78	0.038	0.022	0.29
US	Consumer	1960:01	1995:08	0.23	3.68 3.13	0.77	0.989	0.034	0.80
	Non-Durables	1960:01	1995:08	0.25	3.26	0.84	0.823	0.123 0.332	0.21
	Intermediate	1960:01	1995:08	0.25	2.77	0.70	0.648	0.166	0.34
	Investment	1960:01	1995:08	0.34	2.32	0.58	0.790	0.885	0.80
	Manutacturing Raw Materials	1960:01	1995:08	0.31	2.90	0.83	0.542	0.187	0.20
	Total	1960:01	1995:08	0.24	2.51	0.78	0.753	0.050	0.20
								1	

APPENDIX II

Calculation of Monthly Seasonal Mean Deviations

Consider, firstly, the linear autoregressive process for monthly data such that

$$\phi(L)[y_{i} - \mu_{i}] = \varepsilon_{i} \tag{A.1}$$

means follow a twelve month cycle such that where $\phi(L)$ is a pth order polynomial with all roots outside the unit circle, $E[y_t] = \mu_t$ and the

$$\mu_j = \mu_{j\pm 12n}, \qquad j = 1, ..., 12; n = 1, 2, ...$$
 (A.2)

Therefore, (A.1) and (A.2) define a process y_t which is stationary around the monthly seasonal means $\mu_{1,...},\mu_{12}$.

This can be compared with the usual representation in terms of a seasonal intercept, namely

$$\phi(L)y_{t} = \sum_{j=1}^{12} \delta_{j} D_{jt} + \varepsilon_{t}$$
(A.3)

in which D_{jt} is the conventional dummy variable for month j. Equation (A.3) defines a special case of a periodic process, which has a mean that is a nonlinear function of all seasonal intercepts and autoregressive coefficients; see Ghysels and Osborn (2001, pp.146/147). Equivalence of the two representations follows from stationarity, and hence

$$\mu_j - \sum_{i=1}^{p} \phi_i \mu_{j-i} = \delta_j, \qquad j = 1, ..., 12$$
 (A.4)

Given values of the autoregressive coefficients and the seasonal dummy variable coefficients, (A.4) defines a set of linear equations that can be solved for the unknown seasonal means $\mu_{l_1....}\mu_{l_2}$.

side of (A.4) that refer to each specific monthly mean. This yields In order to solve these equations, it is convenient to collect the coefficients on the left-hand

$$\phi_0(1)\mu_j + \sum_{k=1}^{11} \phi_k(1)\mu_{j-k} = \delta_j, \qquad j = 1, ..., 12$$
 (A.5)

$$\phi_0(1) = 1 - \sum_{n=1}^{\lceil p/12 \rceil} \phi_{12n}$$

$$\phi_k(1) = - \sum_{n=0}^{\lceil (p-k)/12 \rceil} \phi_{12n+k}, \quad k = 1, ..., 11$$

and [.] denotes the integer part of the expression in brackets. Therefore, (A.5) can be written as the conventional linear equation system

$$A\mu = \delta \tag{A.6}$$

in which the vectors $\boldsymbol{\mu} = (\mu_1, \dots, \mu_{I2})'$, $\boldsymbol{\delta} = (\delta_1, \dots, \delta_{I2})'$ and the elements of the matrix \boldsymbol{A} are given

$$a_{ij} = \begin{cases} \phi_0(1) & i = j \\ \phi_{i-j}(1) & i > j \\ \phi_{12+i-j}(1) & j > i \end{cases}$$

The monthly means can then be obtained as

$$\mu = A^{-1}\delta. \tag{A.7}$$

In the context of this paper, the δ_j in equation (3) of the text represent the monthly shift in the intercept in the lower regime, so that application of (A.7) to these values yields the monthly

corresponding equation becomes mean deviation from the overall mean in the lower regime. For the upper regime, the

$$\mu = A^{-1}(\delta + \gamma). \tag{A.8}$$

and upper regimes are obtained as $\phi^{-1}(1)\delta_0$ and $\phi^{-1}(1)[\delta_0 + \gamma_0]$ respectively. each month compared to the overall mean in the upper regime. The overall means for the lower where $\gamma = (\gamma_1, ..., \gamma_{12})'$, with the interpretation that the values represent the mean deviations for

(1993) in the context of a Markov-switching model. representations analogous to (A.1) and (A.3) are not equivalent; this is discussed by Hamilton Finally, as mentioned in the text, it should be noted that the regime-dependent means and monthly mean shifts derived from equation (3) are steady state values. That is, their computation assumes that the regime does not change over time. When a regime switch occurs, the

Figure 1. Estimated Monthly Means in the Upper (indicated by ■) and Lower Regimes











