What is Latent Class Analysis

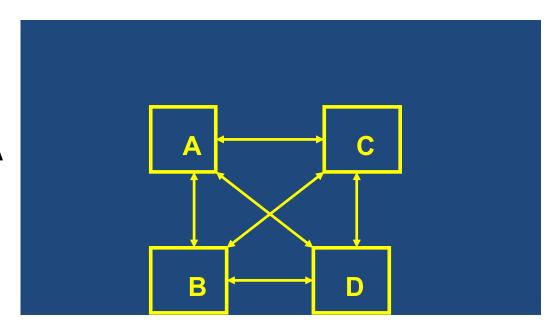
Tarani Chandola methods@manchester

Many names- similar methods

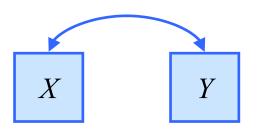
- (Finite) Mixture Modeling
- Latent Class Analysis
- Latent Profile Analysis

Latent class analysis (LCA)

- LCA is a similar to factor analysis, but for categorical responses.
- Like factor analysis, LCA addresses the complex pattern of association that appears among observations....

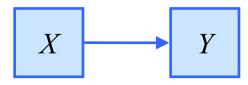


Factor Analysis

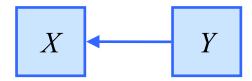


We observe a correlation between two variables. Why?

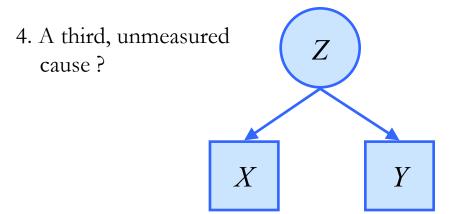
1. X causes Y?



2. Y causes X?



3. Reciprocal causation $(X \leftrightarrow Y)$?



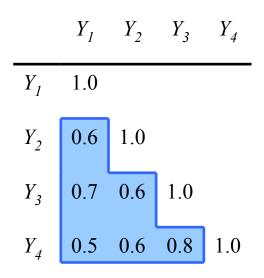
Unmeasured Causes: Factor Models

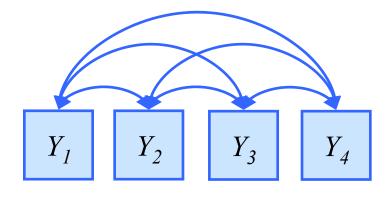
Variables may be related due to the action of unobserved influences.

Sometimes these are confounding variables, but many constructs of interest are not directly observed (or even observable)

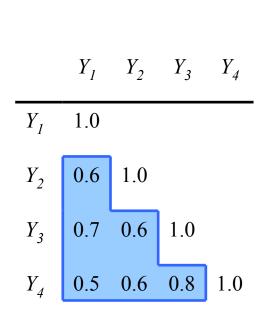
| Unobserved Construct | Observed Measures |
|----------------------|--|
| Social Capital | Bowling club membership Local newspaper reading |
| Ethnic prejudice | Housing segregation Ethnic intermarriage |

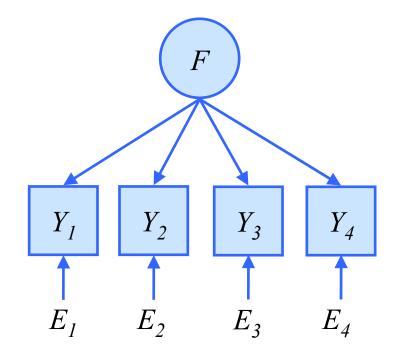
Correlations may not be due to causal relations among the observed variables at all, but due to these unmeasured, latent influences - factors





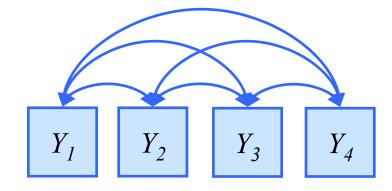
The observed correlations may be due to each observed measure sharing an unobserved component (F)





Example: Four questionnaire items that have highly correlated answers

- Y1 "I Often feel blue"
- Y2 "I dislike myself"
- Y3 "I have a low opinion of myself"
- Y4 "My life lacks direction"



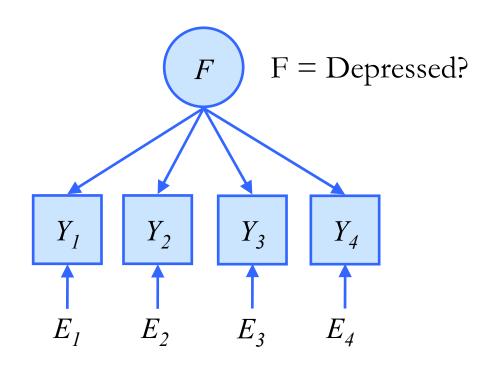
The items may be correlated due to the influence of the respondent's mood state, which we can't observed directly

Y1 "I Often feel blue"

Y2 "I dislike myself"

Y3 "I have a low opinion of myself"

Y4 "My life lacks direction"



| 1 | F | | e1 | e2 | e3 | e4 |
|----|---|-----|------|------|------|------|
| 2 | | 1.2 | -0.4 | 0.2 | -1.5 | -1.4 |
| 3 | | 3.3 | 0.8 | -0.2 | -0.1 | 0.9 |
| 4 | | 2.2 | 0.8 | -1.8 | 0.0 | 1.5 |
| 5 | | 1.3 | 0.6 | -1.9 | 0.3 | 1.0 |
| 6 | | 1.5 | -0.9 | 0.1 | 1.6 | 1.0 |
| 7 | | 1.6 | -1.5 | 1.0 | 0.5 | -0.4 |
| 8 | | 2.2 | 1.5 | 1.2 | -0.7 | 0.7 |
| 9 | | 2.1 | -0.6 | 0.7 | 0.1 | 0.2 |
| 10 | | 0.7 | 0.3 | 0.2 | -0.4 | 1.5 |
| 11 | | 1.9 | 0.5 | -1.3 | 0.2 | -0.1 |

| у1 | | y 2 | у 3 | у4 |
|----|-----|------------|------------|------|
| | 0.8 | 1.4 | -0.3 | -0.2 |
| | 4.1 | 3.1 | 3.2 | 4.2 |
| | 3.0 | 0.4 | 2.2 | 3.7 |
| | 1.9 | -0.6 | 1.6 | 2.3 |
| | 0.6 | 1.6 | 3.1 | 2.5 |
| | 0.1 | 2.6 | 2.1 | 1.2 |
| | 3.7 | 3.4 | 1.5 | 2.9 |
| | 1.5 | 2.8 | 2.2 | 2.3 |
| | 1.0 | 0.9 | 0.3 | 2.2 |
| | 2.4 | 0.6 | 2.1 | 1.8 |

Hypothesised Factor Model

Observed data

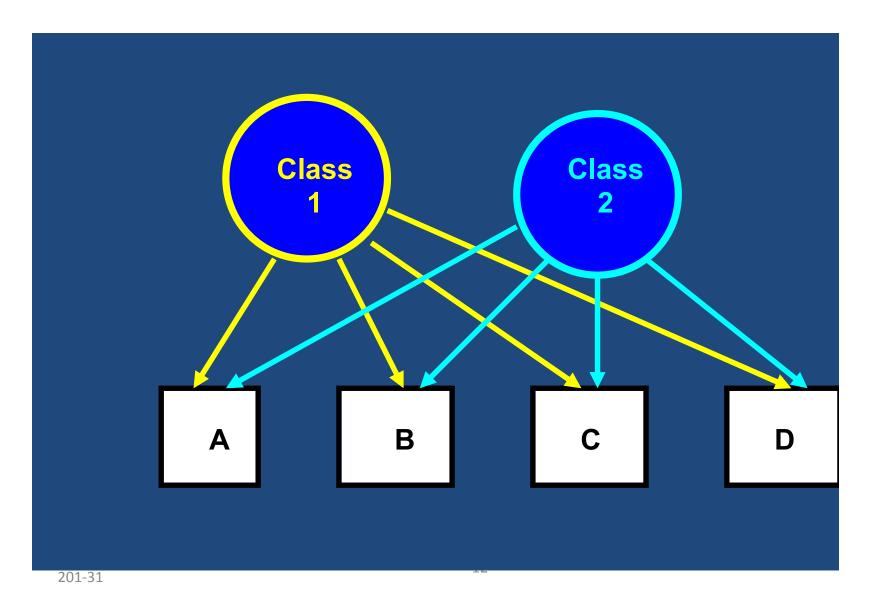
Model Fit

- Standard measure of 'observed' vs. 'expected' fit?
 - Pearson χ^2 (Chi-Square) test
 - Sum of the squared differences between observed
 (O) and expected (E) (co)variances divided by the expected

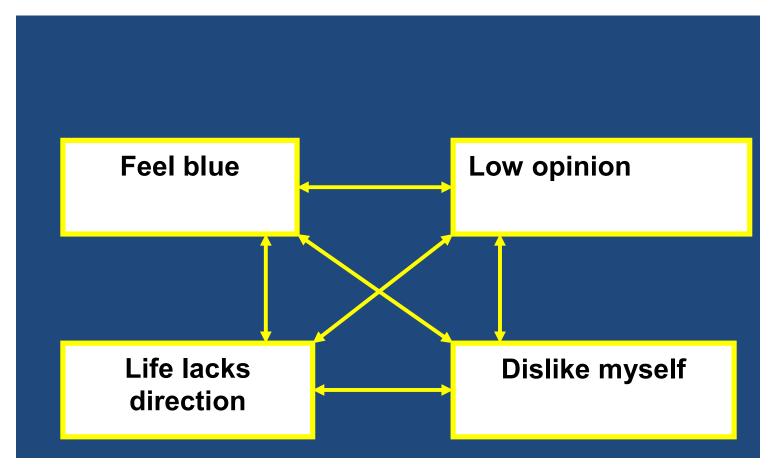
$$\chi^2 = \Sigma[(O-E)^2/E]$$

- The larger the χ^2 the greater the model **mis**fit
- Can test if $\chi^2 = 0$ using the model df

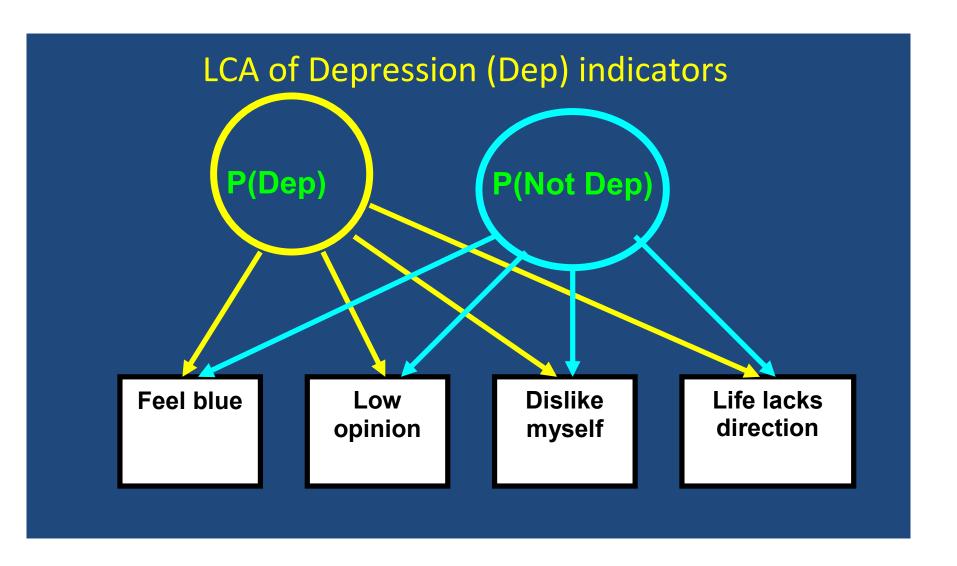
In LCA, the underlying unobserved variables are not continuous (dimensions) but classes/categories/discrete



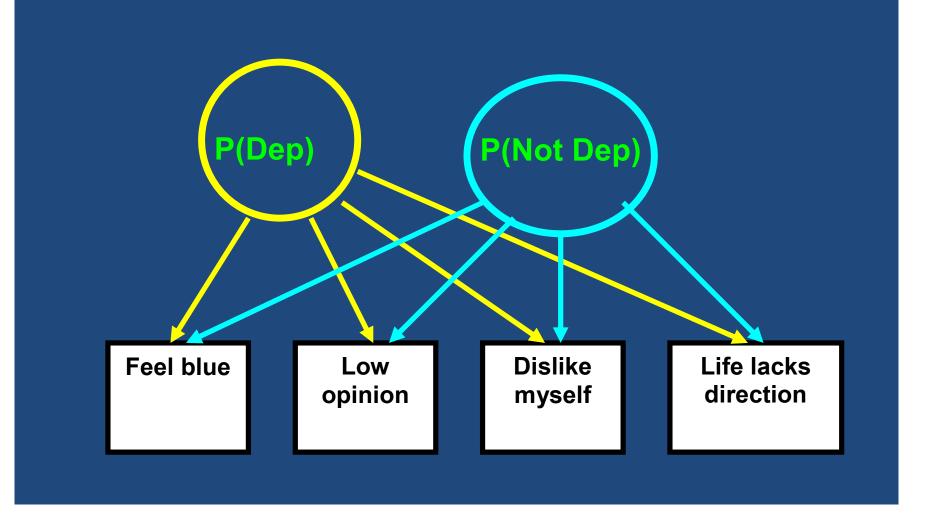
What if you do not know how to classify people into (depressed vs not depressed) groups? What if there is no gold standard to assess a pattern of "yes/no" signs and symptoms?



Rindskopf, R., & Rindskopf, W. (1986). The value of latent class analysis in medical diagnosis. *Statistics in Medicine*, *5*, 21-27.



LCA predicts latent class membership such that the observed variables are independent.



LCA estimates

Latent class prevalences

Conditional probabilities: probabilities of specific response, given class membership

LCA works on unconditional contingency table (no information on latent class membership)

| Feel blue | Low opinion | Dislike myself | Life lacks direction | n _{ijkl} |
|--------------|----------------|-------------------|----------------------|-------------------|
| 0 | 0 | 0 | 0 | 15 |
| 0 | 0 | 0 | 1 | 14 |
| 0 | 0 | 1 | 0 | 11 |
| 0 | 0 | 1 | 1 | 8 |
| 0 | 1 | 0 | 0 | 23 |
| | • | • | • | |
| 1 | 1 | 1 | 1 | 9 |

LCA's goal is to produce a complete (conditional) table that assigns counts for each latent class:

| Feel | Dislike | Low | Life | Latent | n _{ijklt} |
|------|---------|---------|---------------|--------|--------------------|
| blue | myself | opinion | lacks | Class | |
| | | | directi on | X=t | |
| 0 | 0 | 0 | _ | 4 | |
| U | U | 0 | 0 | 1 | 9 |
| 0 | 0 | 0 | 1 | 2 | 6 |
| 0 | 0 | 1 | 0 | 1 | 3 |
| 0 | 0 | 1 | 1 | 2 | 11 |
| | • | • | | • | • |
| 1 | 1 | 1 | 1 | 2 | 9 |

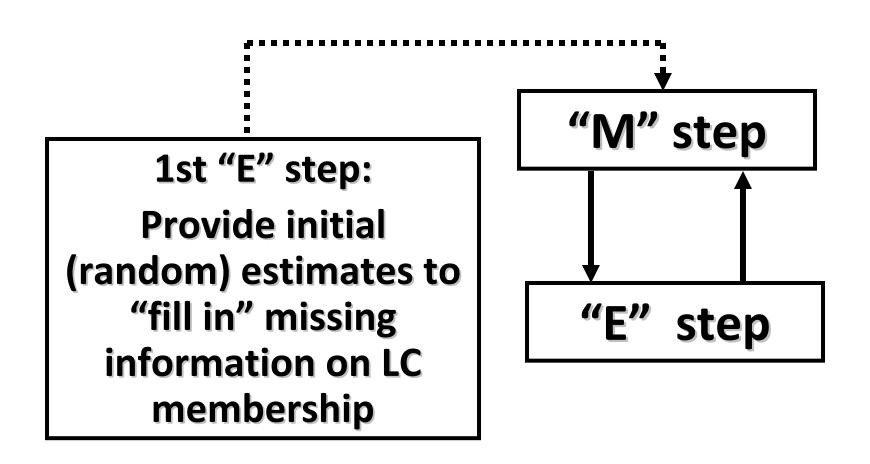
Estimating LC parameters

- Maximum likelihood approach
- Because LC membership is unobserved, the likelihood function, and the likelihood surface, are complex.

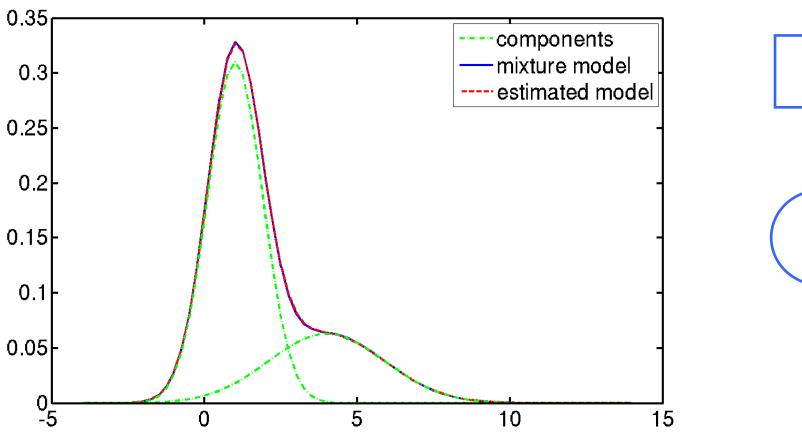
EM algorithm calculates L when some data (X) are unobserved

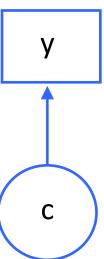
"M" step produces ML estimates from complete table "E" step uses parameter estimates to update expected values for cell counts nijkit in complete contingency table

EM algorithm requires initial estimates

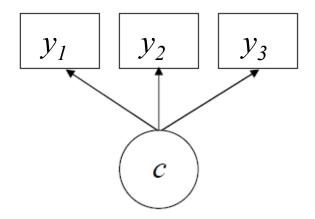


Mixture modeling





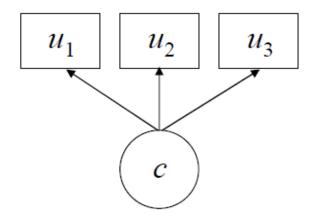
Latent Profile Analysis Model



Continuous indicators

$$y$$
: y_1 , y_2 , ..., y_r
Categorical latent variable
 c : $c = k$; $k = 1, 2, ..., K$.

Latent Class Analysis Model



Dichotomous (0/1) indicators

$$u: u_1, u_2, ..., u_r$$

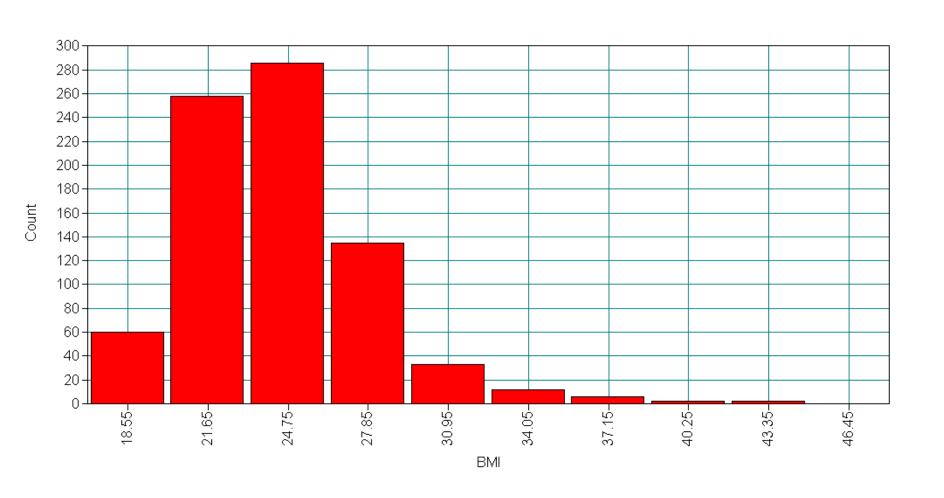
Categorical latent variable $c: c = k; k = 1, 2, ..., K$.

Model Results

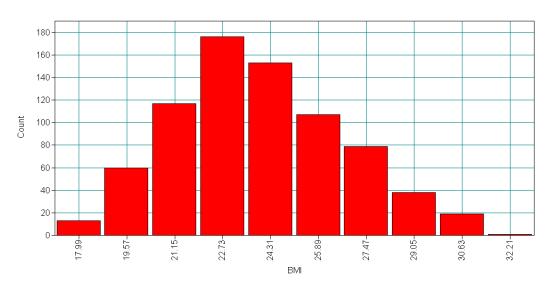
| | Estimate | S.E. | Est./S.E. | Two-Tailed P-Value |
|------------------|----------|-------|-----------|-----------------------|
| Latent Class 1 | | | | |
| Means BMI | 25.166 | 0.139 | 181.262 | 0.000 |
| Variances BMI | 15.305 | 1.279 | 11.970 | 0.000 |

Mean BMI of 25.2 (and variance of 15.3) in the whole population

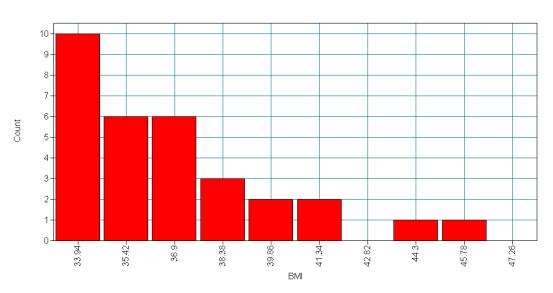
Histogram of BMI (1 class solution)



Class 1



Class 2

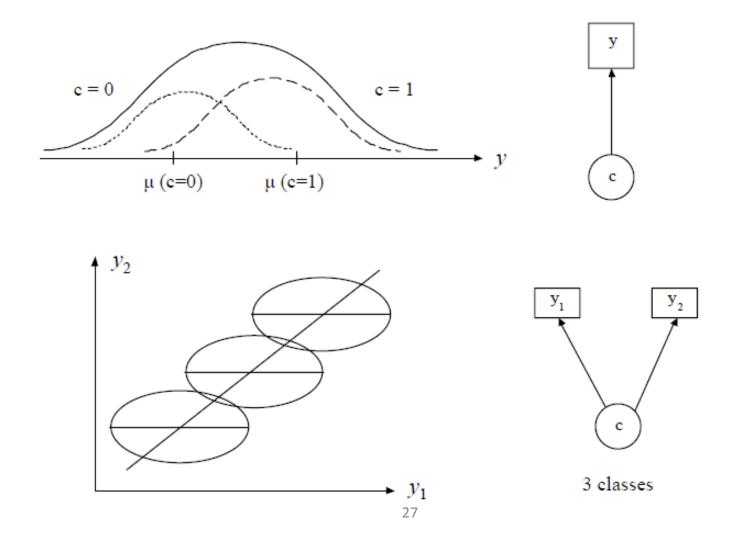


Mixture Model of BMI with 3 classes

| | Estimate | S.E. | Est./S.E. | Two-Tailed P-Value |
|-------------------------|-----------|--------|-----------|-----------------------|
| Latent Class 1 Means | | | | |
| BMI | 32.100 | 16.503 | 1.945 | 0.052 |
| Variances | | | | |
| BMI | 8.319 | 4.653 | 1.788 | 0.074 |
| Latent Class 2 | | | | |
| Means | | | | |
| BMI | 40.685 | 18.724 | 2.173 | 0.030 |
| Variances | | | | |
| BMI | 8.319 | 4.653 | 1.788 | 0.074 |
| Latent Class 3 | | | | |
| Means | | | | |
| BMI | 24.414 | 1.342 | 18.190 | 0.000 |
| Variances | | | | |
| BMI | 8.319 | 4.653 | 1.788 | 0.074 |
| Categorical Latent | Variables | | | |
| Means | | | | |
| C#1 | -2.561 | 2.973 | -0.861 | 0.389 |
| C#2 | -4.277 | 5.878 | -0.728 | 0.467 |

[!] Those in Class 2 have much higher mean BMI than those in classes 1 and 3

Latent Profile/Class analysis with 2 and 3 latent classes

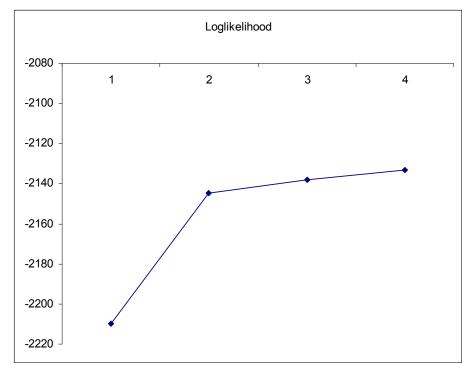


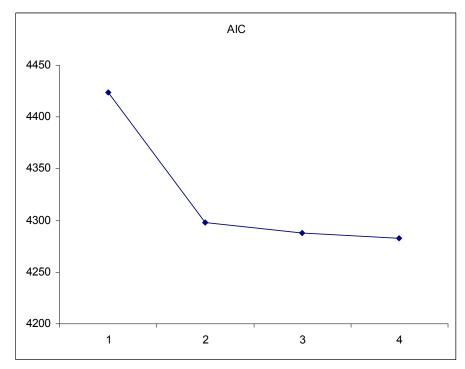
Deciding on number of latent classes

- Start with the simplest (a one class) solution, and add more classes stepwise.
- Examine the model evaluation statistics: Chi-square difference tests are not appropriate for likelihood ratio test comparisons of models with higher numbers of classes. Models that *maximize* the log likelihood are generally better fitting, although this comes at the expense of fitting more parameters to the model. Look for *low* values on the Akaike's Information Criterion (AIC), Bayesian Information Criterion (BIC) and sample size adjusted BIC statistics. In addition, Tech 11: modification to the likelihood ratios test that adjusts the conventional likelihood ratio test for K vs K-1 classes for violation of regularity conditions (*p>0.05* indicates K-1 classes are sufficient).
- Examine entropy measure (higher values indicate better fit).
- Usefulness of the latent classes in practice. This can be determined by examining the trajectory shapes for similarity, the number of individuals in each class, and whether the classes are associated with observed characteristics in an expected manner.

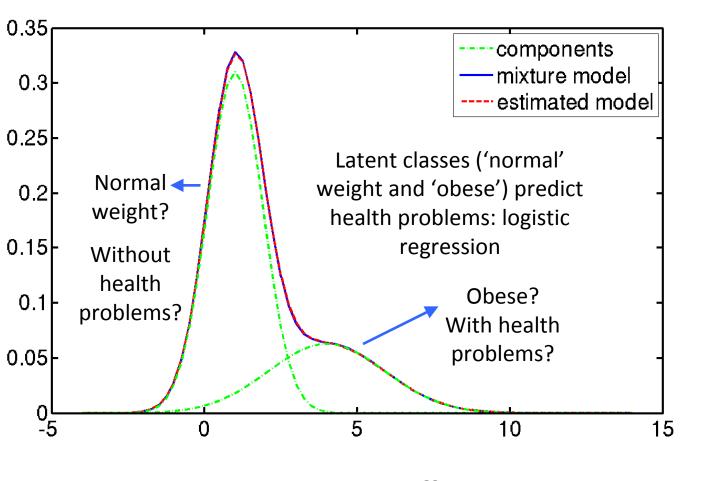
Deciding on number of classes- BMI example

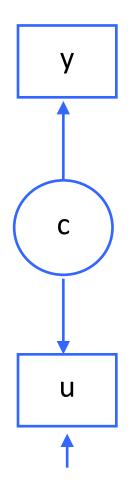
| | | | | | | LRT p-value for |
|----------------|---------------|--------|----------|----------|---------|-----------------|
| No. of classes | Loglikelihood | # par. | AIC | BIC | Entropy | k-1 |
| 1 | -2209.712 | 2 | 4423.424 | 4432.778 | NA | NA |
| 2 | -2144.898 | 4 | 4297.797 | 4316.505 | 0.952 | 0.0000 |
| 3 | -2137.826 | 6 | 4287.652 | 4315.714 | 0.901 | 0.8237 |
| 4 | -2133.359 | 8 | 4282.718 | 4320.135 | 0.745 | 0.0326 |



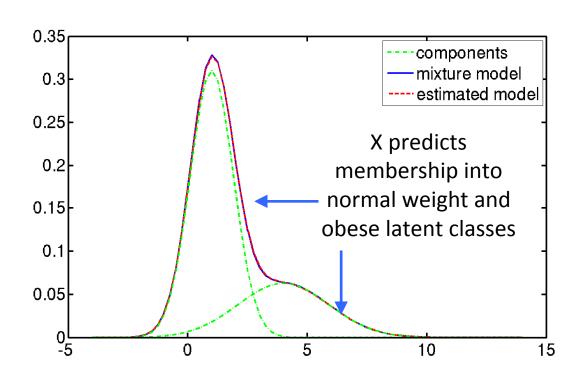


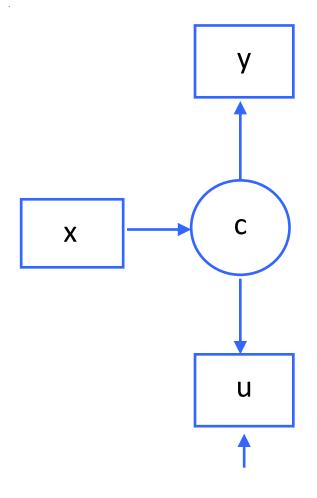
Mixture modeling with categorical dependent variables



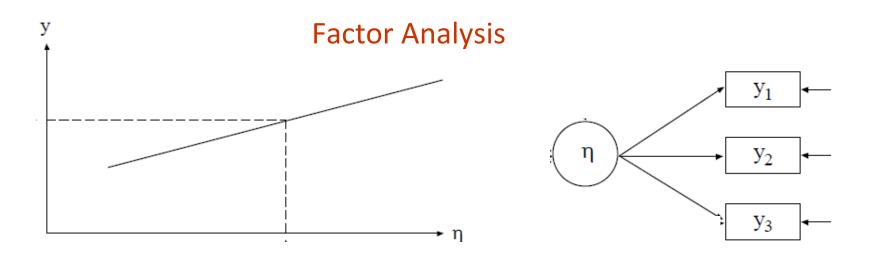


Mixture model with covariates and categorical dependent variables

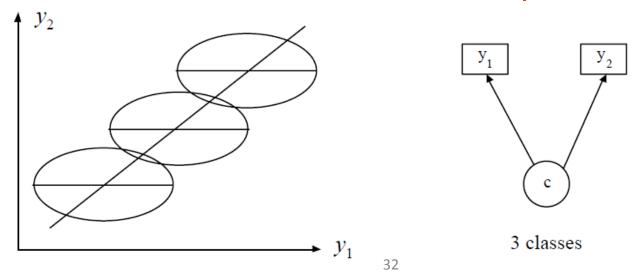




Are you a joiner or a splitter?



vs. Latent Profile/Class Analysis



Resources

Introduction to LCA:

http://www.john-uebersax.com/stat/faq.htm

http://www.ccsr.ac.uk/methods/festival/programme/wiwp/francis.pdf

McCutcheon AC. Latent class analysis. Beverly Hills: Sage Publications, 1987

Software:

http://www.john-uebersax.com/stat/soft.htm

Short courses:

Latent Trait and Latent Class Analysis for Multiple Groups Using Mplus http://www.ccsr.ac.uk/courses/congnitiveInterviewing/LatT.html

Introduction to Structural Equation Modelling using Mplus http://www.ccsr.ac.uk/courses/semintro/